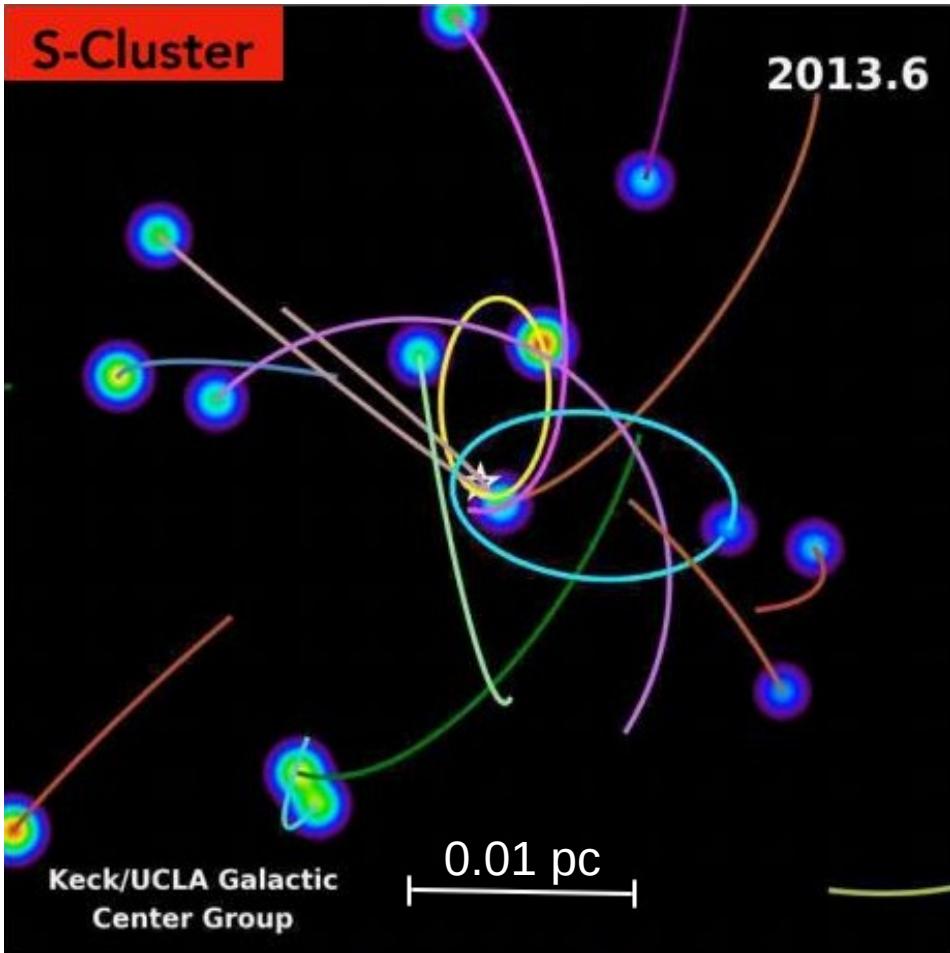


Scalar resonant relaxation with IMBH

Probing the Galactic center's cluster with scalar resonant relaxation

Kerwann Tep

Context

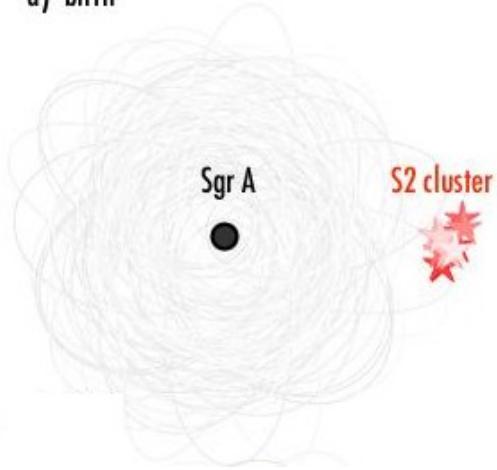


Orbits of S-cluster's stars near Sgr A*

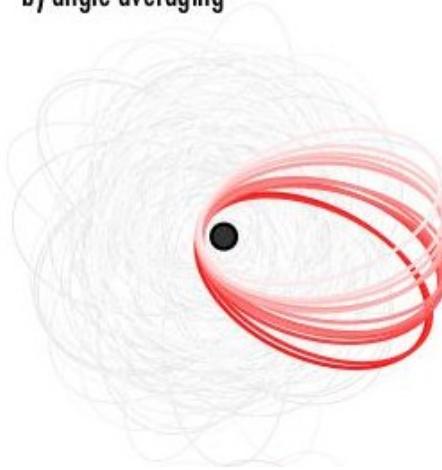
- Galactic center and S-Cluster
 - Fast Keplerian orbits
 - High density of stars
 - Supermassive black hole (SMBH) Sgr A*
- Formation
 - Intermediate mass black holes (IMBH) ?
 - Mass segregation
- Accessible data
 - GAIA
 - VLT (through the instrument Gravity)

Dynamics and time scales

a) birth



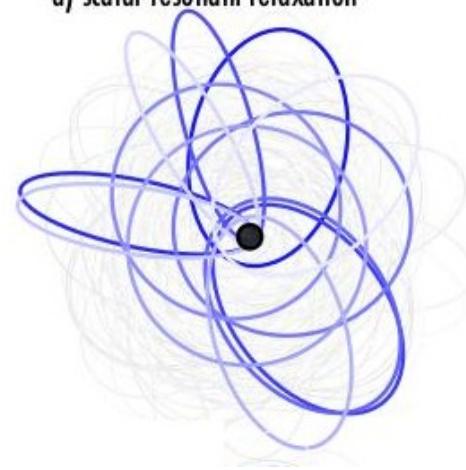
b) angle averaging



c) phase mixing

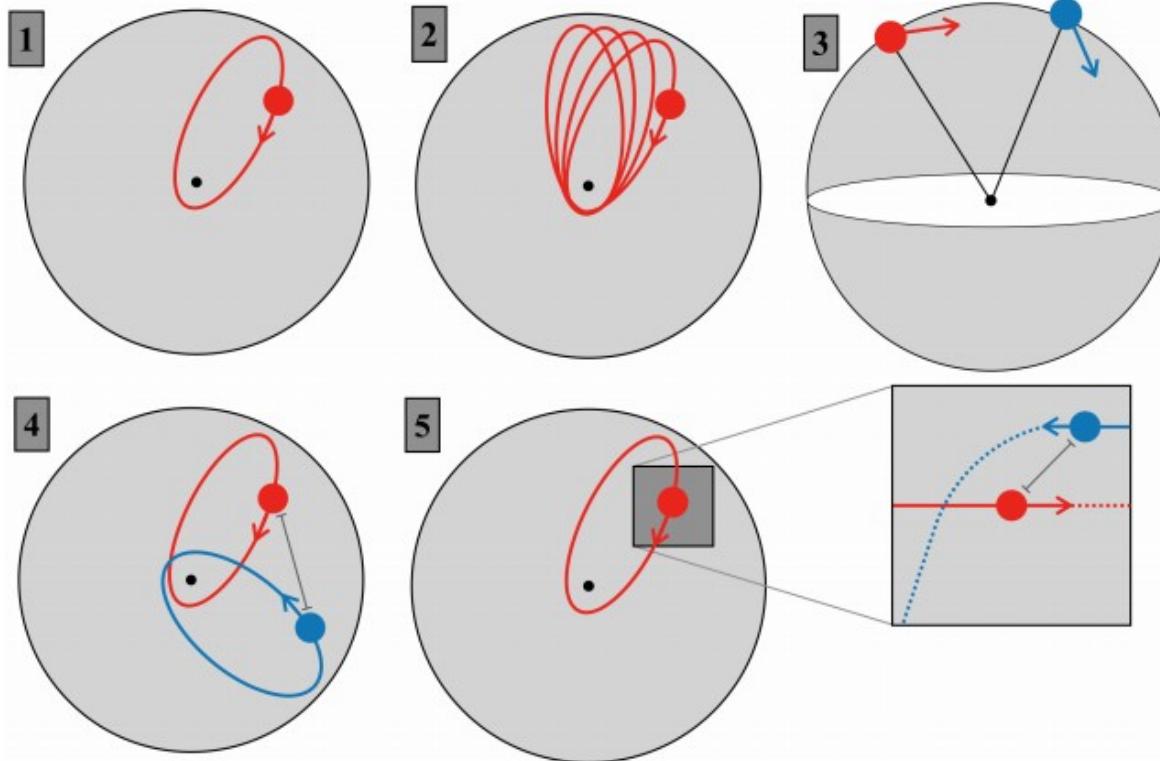


d) scalar resonant relaxation



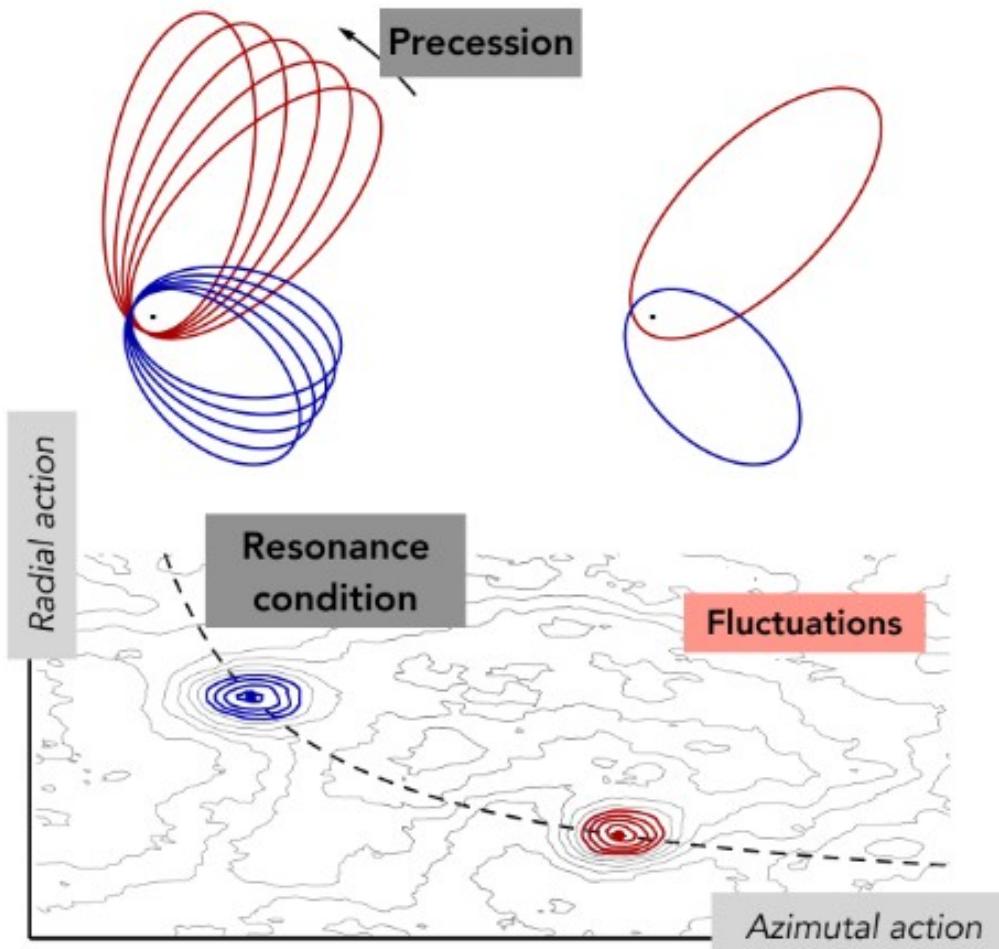
- Constrain the SMBH diet
- Invisible matter experiment
- Five processes influence stars' orbits : from orbital time to secular time

Dynamics and time scales



- 1) Orbital time
- 2) Precession time
- 3) VRR time
- 4) SRR time
- 5) NR time

Scalar resonant relaxation



$$\frac{\partial P}{\partial t} = \frac{1}{2} \frac{\partial}{\partial j} \left[j D_{jj} \frac{\partial}{\partial j} \left(\frac{P}{j} \right) \right]$$

- Poisson noise
 - Finite-N effects
- Non-local resonances
 - Commensurable frequencies
 - Strong correlation
- Sources orbital diffusion

SRR diffusion

$$D_{jj}(\mathbf{J}) \propto \frac{1}{N_*} \sum_{n,n'} n^2 \int da' dj' F_{\text{tot}}(a', j') |A_{nn'}(a, j, a', j')|^2 \\ \times \delta_D(n\nu_P(a, j) - n'\nu_P(a', j'))$$

$D_{jj}(\mathbf{J})$ Anisotropic diffusion

$|A_{nn'}(a, j, a', j')|^2$ Coupling coefficient

$\delta_D(n\nu_P(a, j) - n'\nu_P(a', j'))$ Resonance condition

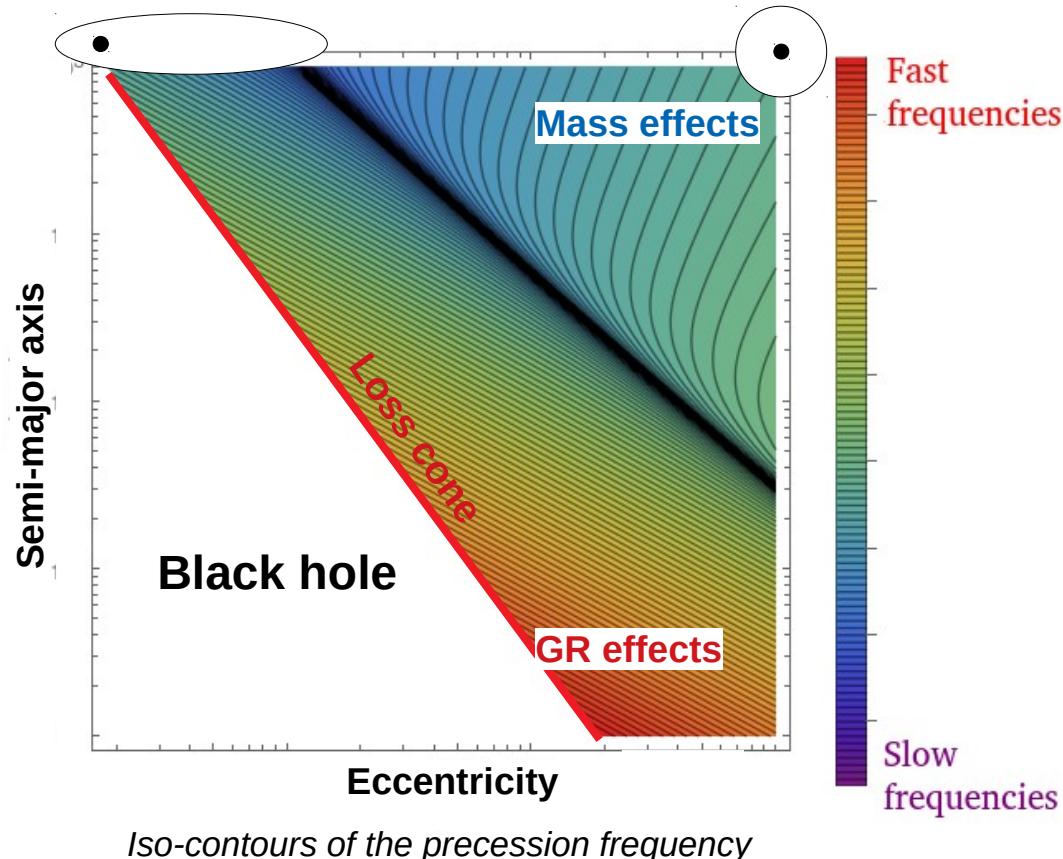
$1/N_*$ Finite-N effects

n^2 Resonance numbers

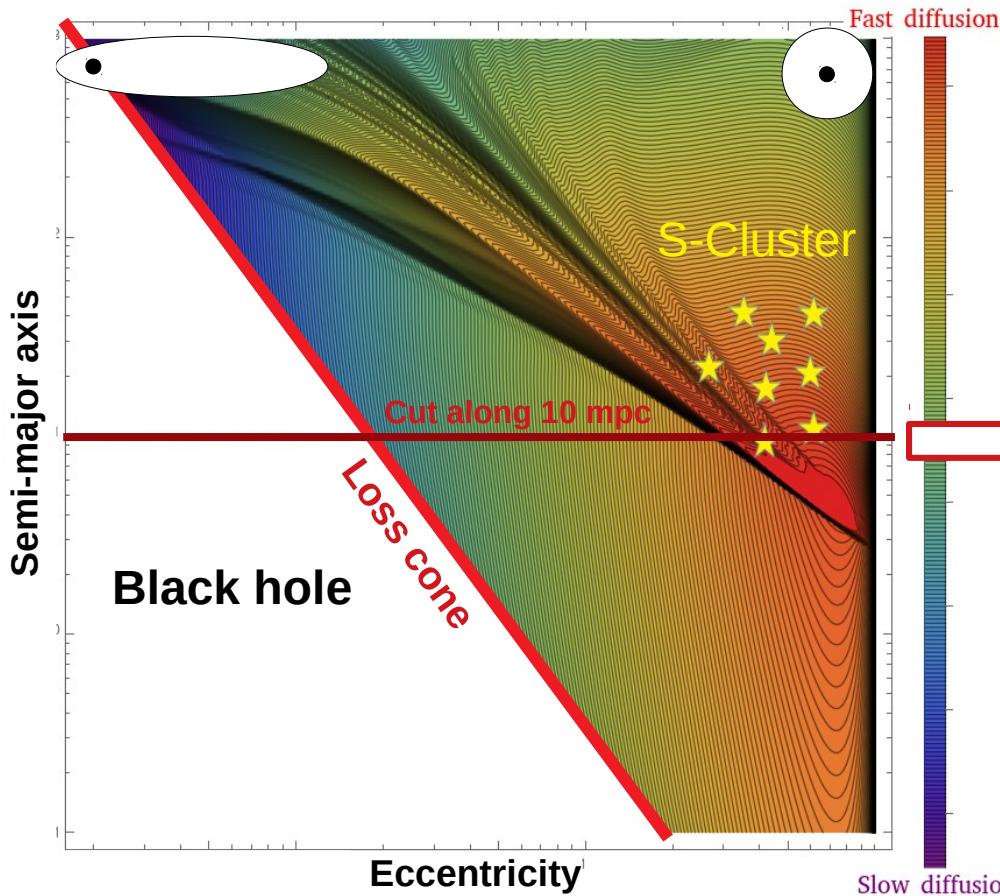
$F_{\text{tot}}(a', j')$ Invisible cluster distribution function

Resonance line

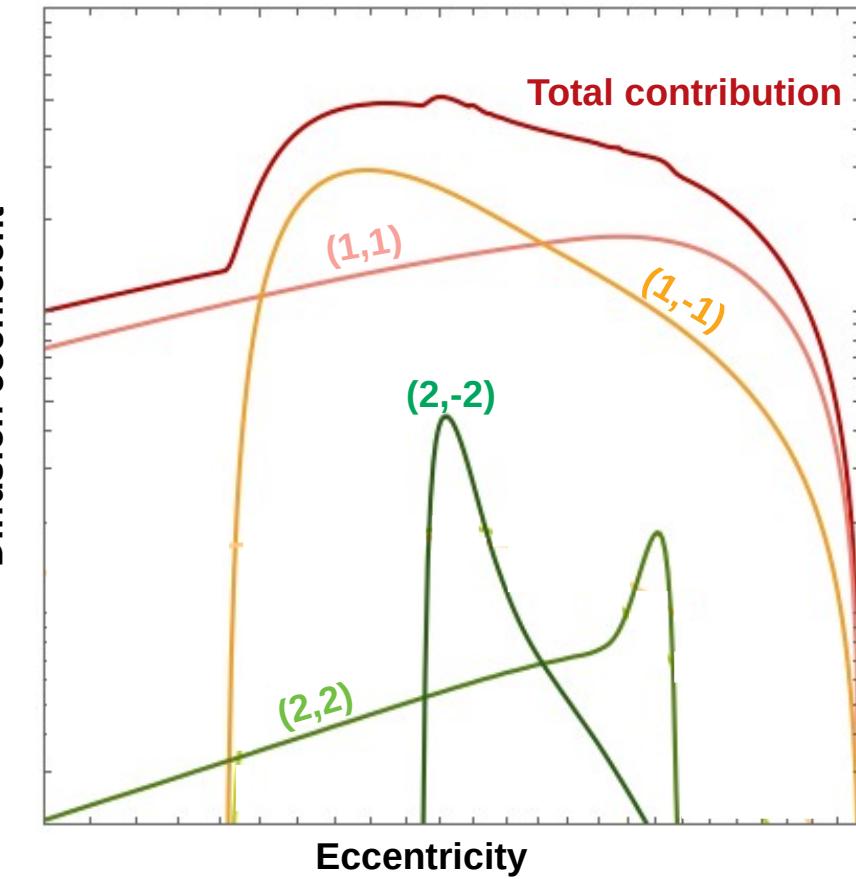
- Precession : 2 contributions
 - Relativistic (BH) effects
 - Invisible cluster's mass
- Asymptotic behaviours :
 - GR effects
(very elliptic orbits close to BH)
 - Cluster mass effects
(circular orbits away from BH)
- Loss-cone
 - Stars fall into the BH



Diffusion coefficients



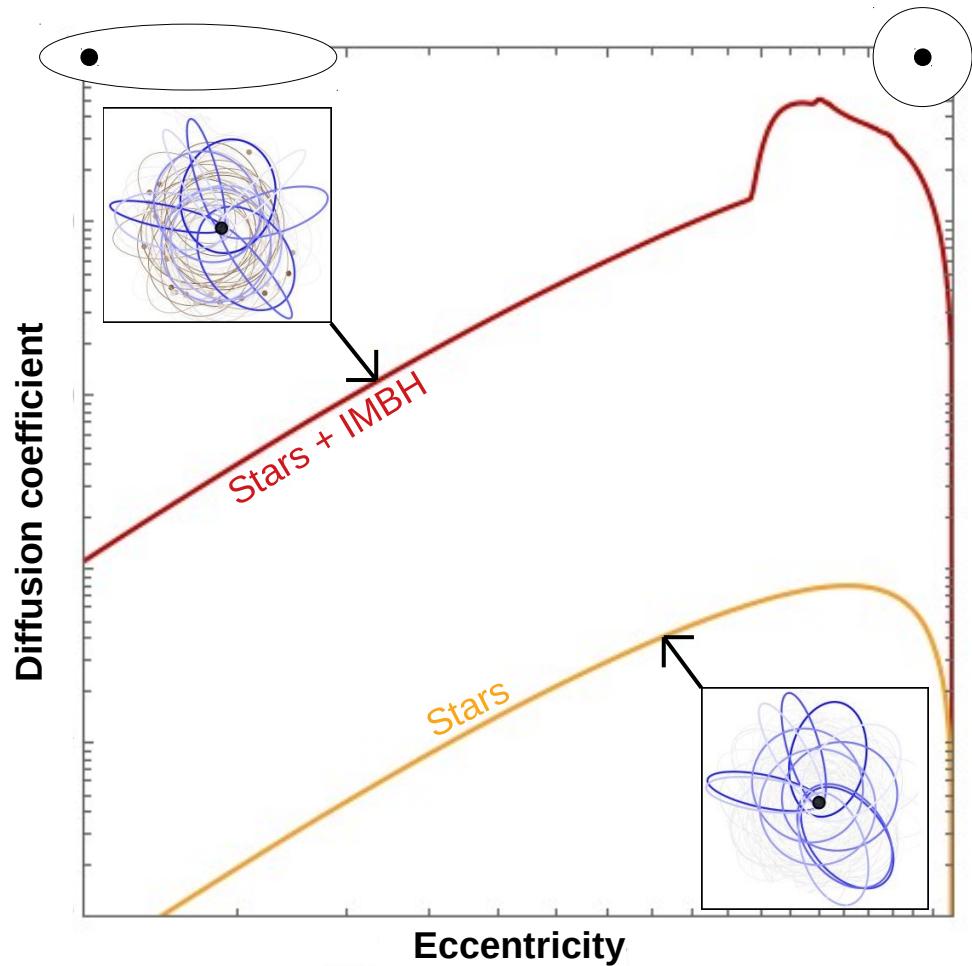
SRR Diffusion coefficients



Contribution of each resonances

Comparing two cluster models

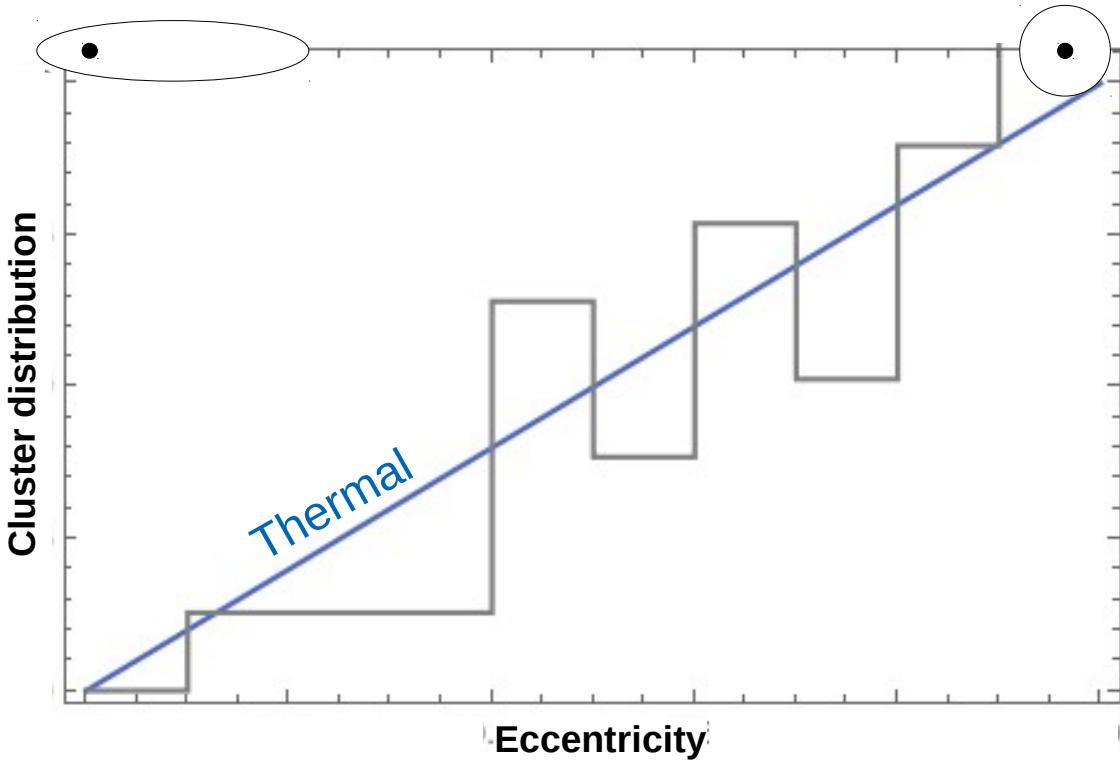
- Model-dependent
 - IMBHs increase efficiency
 - Different resonances
- Efficient computation
 - Parallelized code
 - Linear (sampling) time
 - Exploration of parameter space (add more curves)



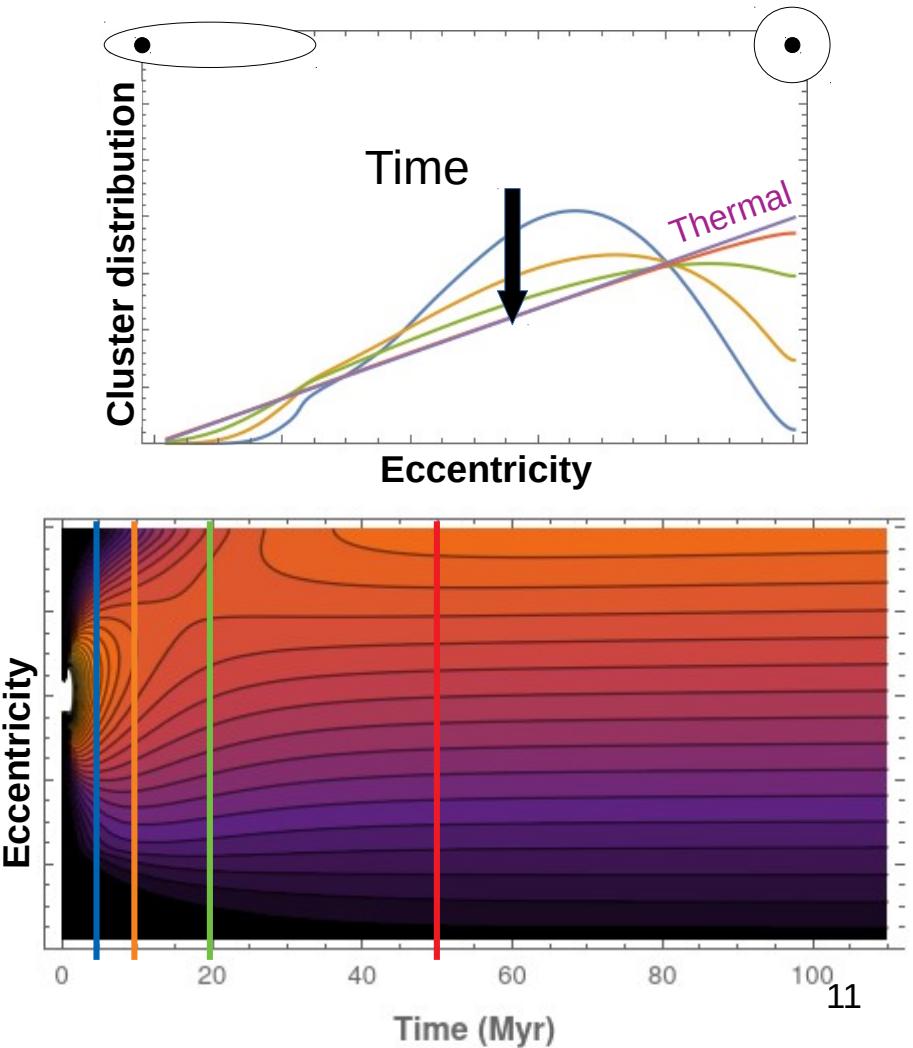
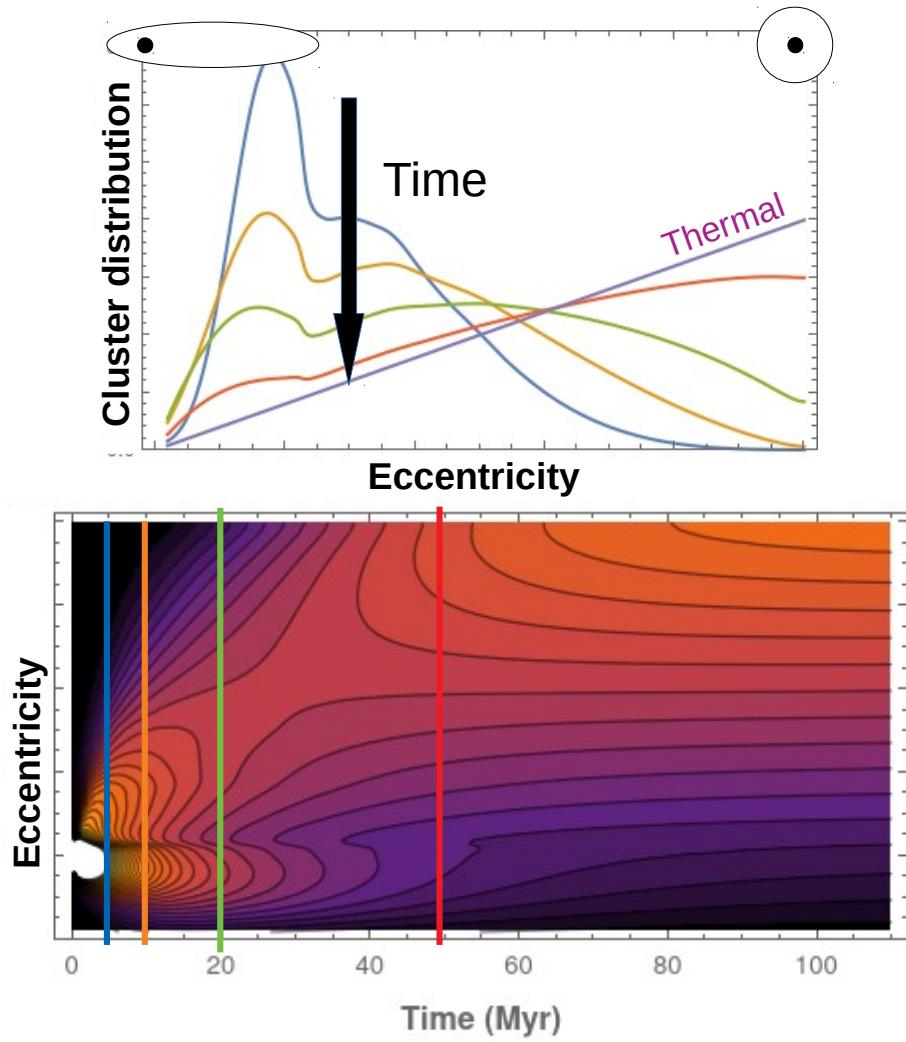
Observations

$$\frac{\partial P}{\partial t} = \frac{1}{2} \frac{\partial}{\partial j} \left[j D_{jj} \frac{\partial}{\partial j} \left(\frac{P}{j} \right) \right]$$

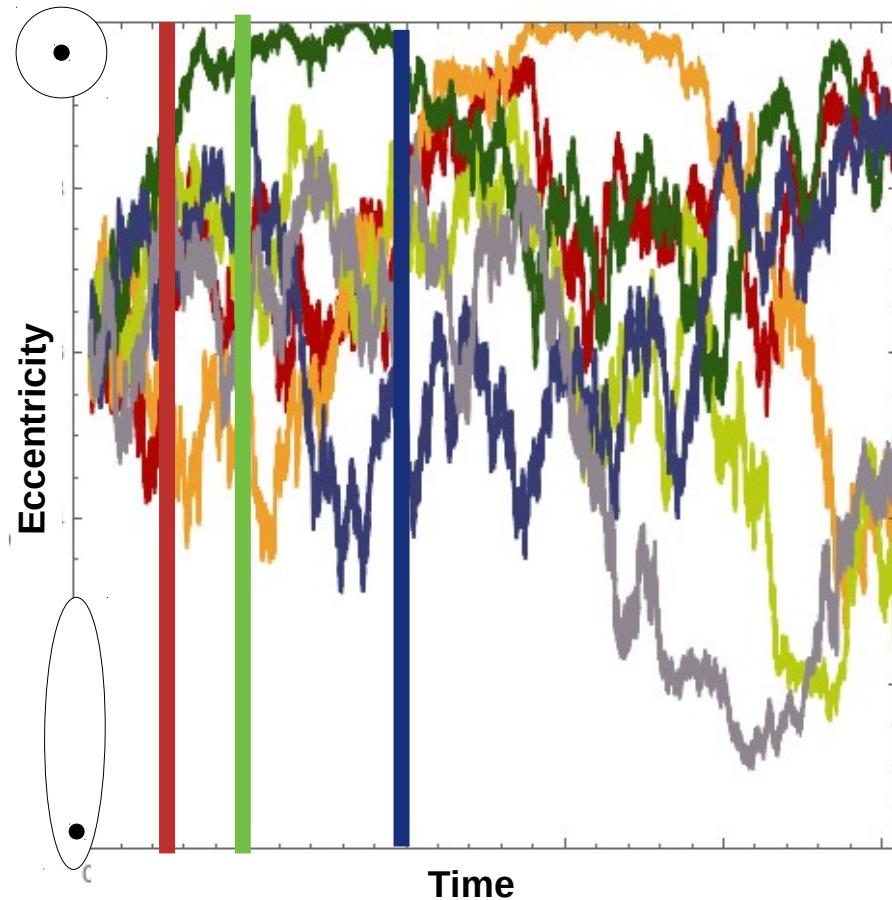
- Diffusion equation of the PDF
 - Equilibrium : $P(j) = 2 j$
- Thermalization of stars
 - Diffusion must be efficient



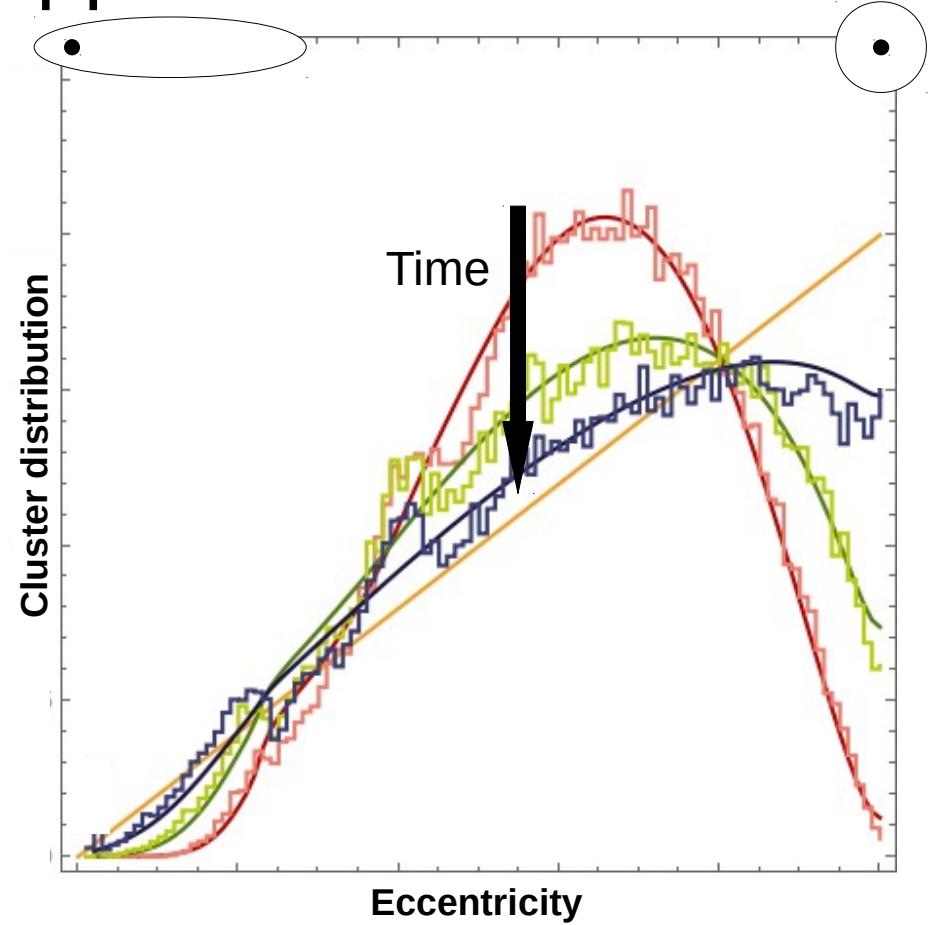
Diffusion equation integration



Stochastic approach

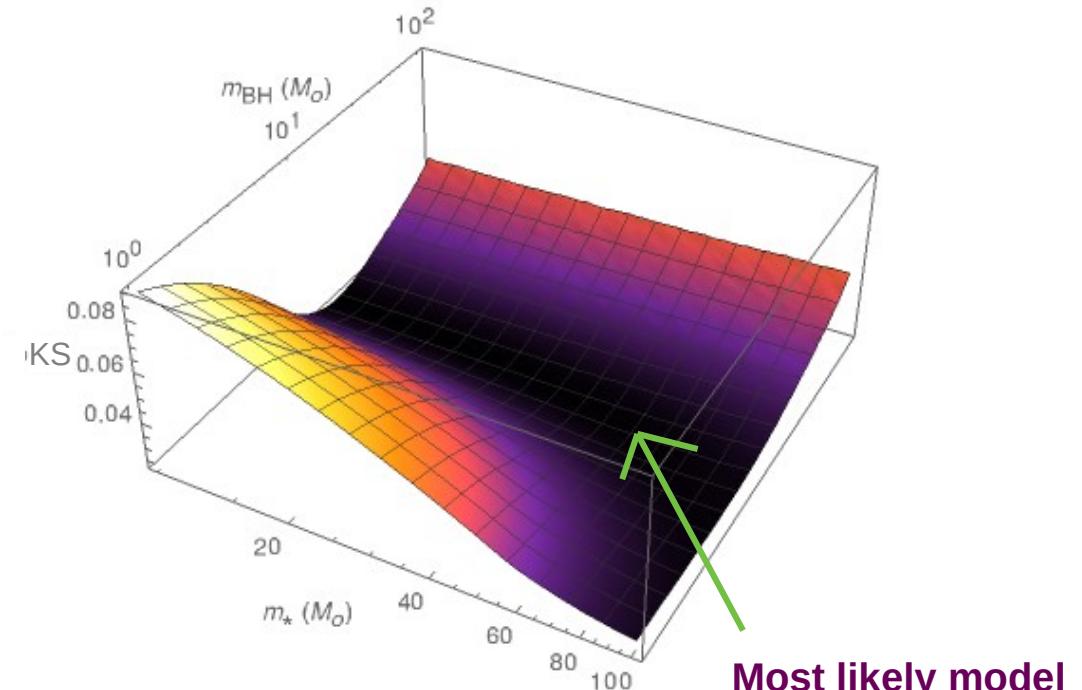
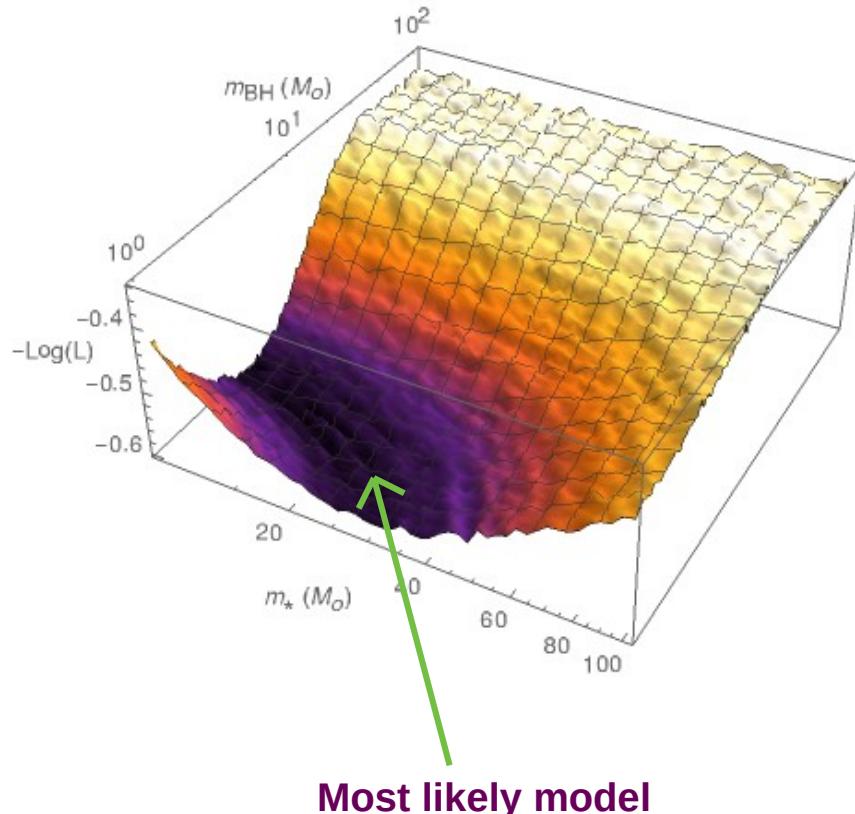


$$\Delta j_t = D_j \Delta t + \sqrt{D_{jj} \Delta t} \xi_t$$



→ Monte-Carlo process

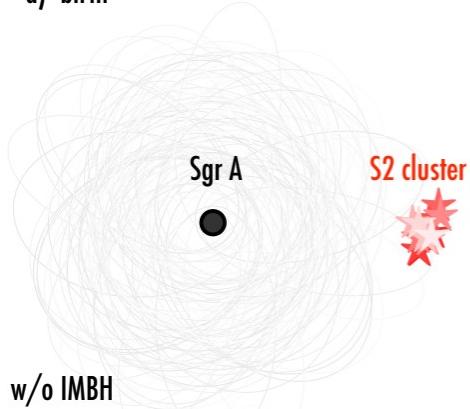
Constraining the models



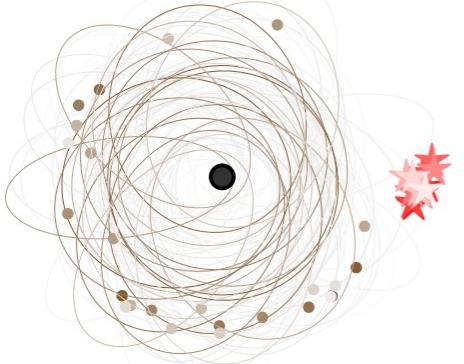
→ We can constrain the models

Conclusions

a) birth

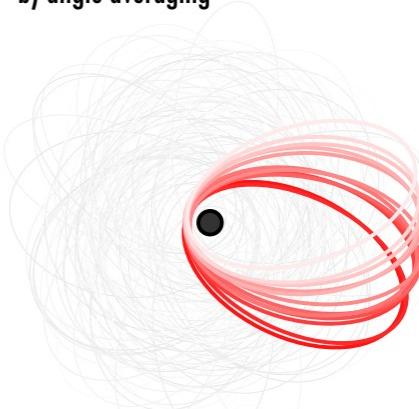


w/o IMBH

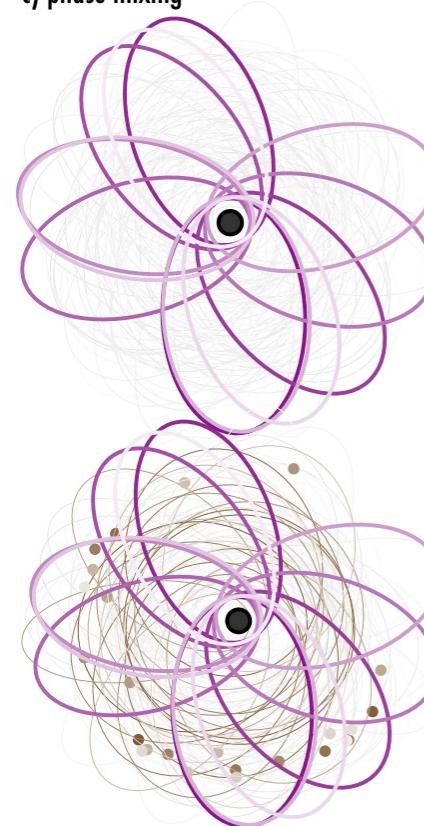


with IMBH

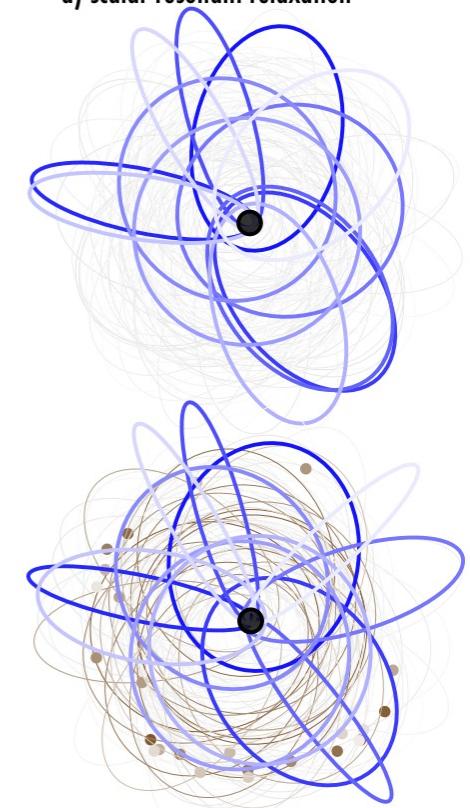
b) angle averaging



c) phase mixing

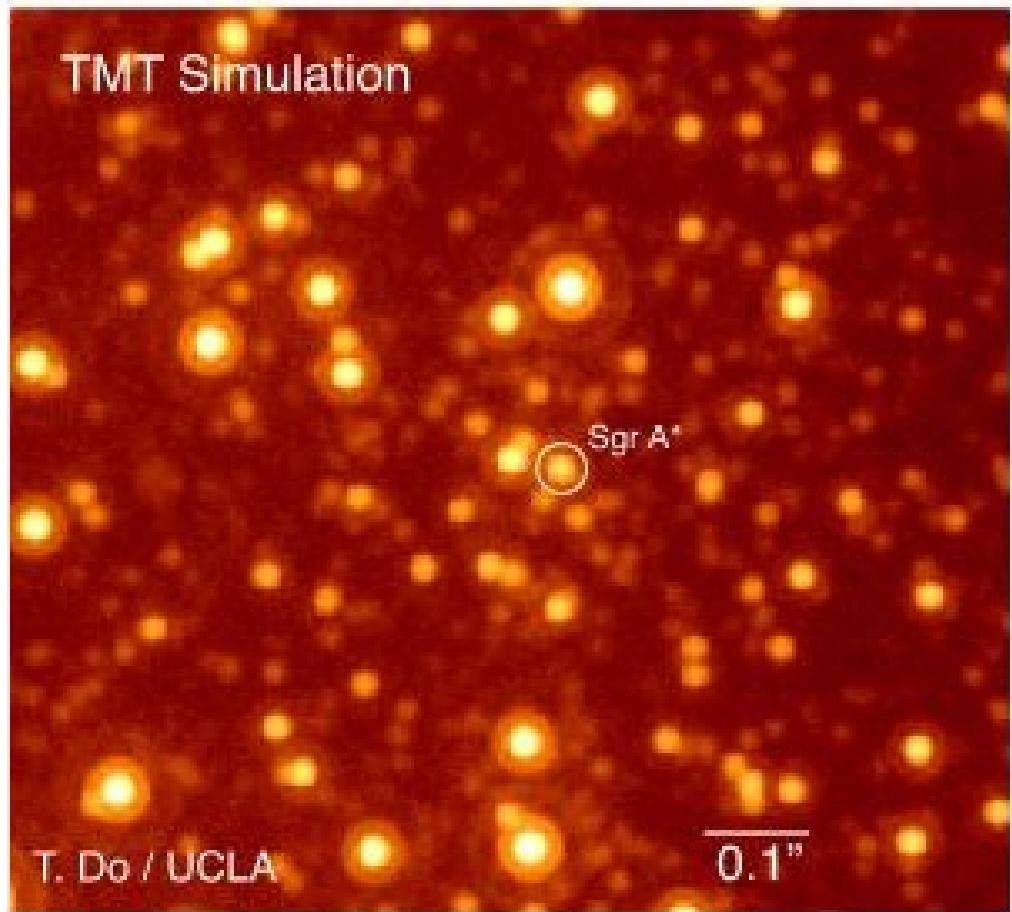
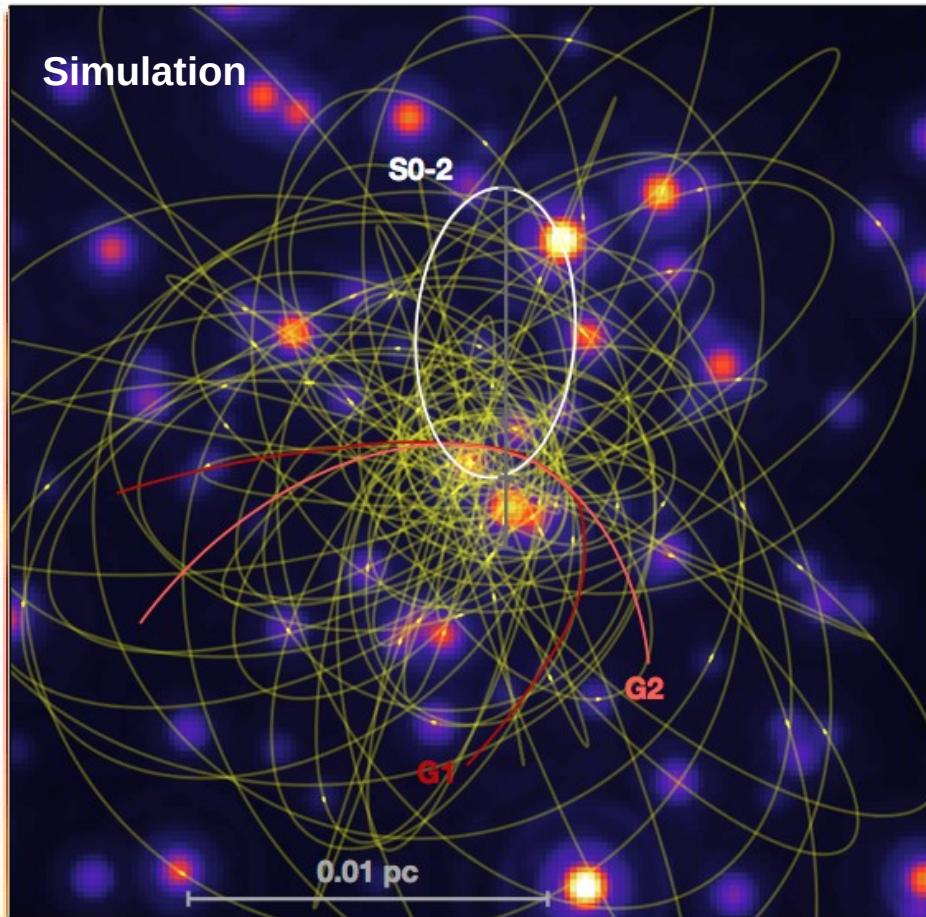


d) scalar resonant relaxation



Secular evolution with and without IMBH

Perspectives



Last slide : key infos+images